Universal Gravitation Practice Problems

Universal Gravitation: \( F_G = \frac{G m_1 m_2}{r^2} \), \( G = 6.67 \times 10^{-11} \text{Nm}^2/\text{kg}^2 \)

Class Work

1. Two spherical objects have masses of 200 kg and 500 kg. Their centers are separated by a distance of 25 m. Find the gravitational attraction between them.

2. Two spherical objects have masses of 1.5 \( \times 10^5 \) kg and 8.5 \( \times 10^2 \) kg. Their centers are separated by a distance of 2500 m. Find the gravitational attraction between them.

3. Two spherical objects have masses of 3.1 \( \times 10^5 \) kg and 6.5 \( \times 10^3 \) kg. The gravitational attraction between them is 65 N. How far apart are their centers?

4. Two spherical objects have equal masses and experience a gravitational force of 25 N towards one another. Their centers are 36 cm apart. Determine each of their masses.

5. A 1 kg object is located at a distance of 6.4 \( \times 10^6 \) m from the center of a larger object whose mass is 6.0 \( \times 10^{24} \) kg.
   a. What is the size of the force acting on the smaller object?
   b. What is the size of the force acting on the larger object?
   c. What is the acceleration of the smaller object when it is released?
   d. What is the acceleration of the larger object when it is released?

Homework

6. Two spherical objects have masses of 8000 kg and 1500 kg. Their centers are separated by a distance of 1.5 m. Find the gravitational attraction between them.

7. Two spherical objects have masses of 7.5 \( \times 10^5 \) kg and 9.2 \( \times 10^7 \) kg. Their centers are separated by a distance of 2.5 \( \times 10^3 \) m. Find the gravitational attraction between them.

8. Two spherical objects have masses of 8.1 \( \times 10^2 \) kg and 4.5 \( \times 10^8 \) kg. The gravitational attraction between them is \( 1.9 \times 10^{-3} \) N. How far apart are their centers?

9. Two spherical objects have equal masses and experience a gravitational force of 85 N towards one another. Their centers are 36 mm apart. Determine each of their masses.

10. A 1 kg object is located at a distance of 7.0 \( \times 10^8 \) m from the center of a larger object whose mass is 2.0 \( \times 10^{30} \) kg.
    a. What is the size of the force acting on the smaller object?
    b. What is the size of the force acting on the larger object?
    c. What is the acceleration of the smaller object when it is released?
    d. What is the acceleration of the larger object when it is released?

11. Two spherical objects have masses of 8000 kg and 5.0 kg. Their centers are separated by a distance of 1.5 m. Find the gravitational attraction between them.

12. Two spherical objects have masses of 9.5 \( \times 10^8 \) kg and 2.5 kg. Their centers are separated by a distance of 2.5 \( \times 10^6 \) m. Find the gravitational attraction between them.

13. Two spherical objects have masses of 6.3 \( \times 10^3 \) kg and 3.5 \( \times 10^4 \) kg. The gravitational attraction between them is \( 6.5 \times 10^{-3} \) N. How far apart are their centers?
14. Two spherical objects have equal masses and experience a gravitational force of 25 N towards one another. Their centers are 36 cm apart. Determine each of their masses.

15. A 1 kg object is located at a distance of $1.7 \times 10^6$ m from the center of a larger object whose mass is $7.4 \times 10^{22}$ kg.
   a. What is the size of the force acting on the smaller object?
   b. What is the size of the force acting on the larger object?
   c. What is the acceleration of the smaller object when it is released?
   d. What is the acceleration of the larger object when it is released?

*Gravitational Field: $g = \frac{GM}{r^2}$

Class Work
16. Compute $g$ at a distance of $4.5 \times 10^7$ m from the center of a spherical object whose mass is $3.0 \times 10^{23}$ kg.

17. Compute $g$ for the surface of the moon. Its radius is $1.7 \times 10^8$ m and its mass is $7.4 \times 10^{22}$ kg.

18. Compute $g$ for the surface of a planet whose radius is twice that of the Earth and whose mass is the same as that of the Earth.

19. Compute $g$ for the surface of the sun. Its radius is $7.0 \times 10^8$ m and its mass is $2.0 \times 10^{30}$ kg.

20. Compute $g$ for the surface of Mars. Its radius is $3.4 \times 10^8$ m and its mass is $6.4 \times 10^{23}$ kg.

21. Compute $g$ at a height of $6.4 \times 10^5$ m ($R_E$) above the surface of Earth.

22. Compute $g$ at a height of $2 \, R_E$ above the surface of Earth.

23. Compute $g$ for the surface of a planet whose radius is half that of the Earth and whose mass is double that of the Earth.

Homework
24. Compute $g$ at a distance of $8.5 \times 10^9$ m from the center of a spherical object whose mass is $5.0 \times 10^{28}$ kg.

25. Compute $g$ at a distance of $7.3 \times 10^8$ m from the center of a spherical object whose mass is $3.0 \times 10^{27}$ kg.

26. Compute $g$ for the surface of Mercury. Its radius is $2.4 \times 10^8$ m and its mass is $3.3 \times 10^{23}$ kg.

27. Compute $g$ for the surface of Venus. Its radius is $6.0 \times 10^8$ m and its mass is $4.9 \times 10^{24}$ kg.

28. Compute $g$ for the surface of Jupiter. Its radius of is $7.1 \times 10^7$ m and its mass is $1.9 \times 10^{27}$ kg.

29. Compute $g$ at a height of $4 \, R_E$ above the surface of Earth.

30. Compute $g$ at a height of $5 \, R_E$ above the surface of Earth.

31. Compute $g$ for the surface of a planet whose radius is double that of the Earth and whose mass is also double that of the Earth.
**Orbital Motion: \( \frac{T^2}{r^3} = \frac{4\pi^2}{GM^1}, v = \sqrt{\frac{GM}{r}} \), \( R_E = 6.4\times10^6 \) m

Class Work

32. Compute:
   a. The velocity of an object orbiting at a distance of \( 4.5 \times 10^7 \) m from the center of a spherical object whose mass is \( 3.0 \times 10^{23} \) kg.
   b. Compute the orbital period of that object.

33. Compute:
   a. The velocity of an object orbiting at a height of \( 6.4 \times 10^6 \) m above the surface of Earth.
   b. Compute the orbital period of that object.

34. Mars has two moons, Phobos and Deimos. Phobos has an orbital radius of \( 9.4 \times 10^6 \) m and an orbital period of 0.32 days. Deimos has an orbital radius of \( 23.5 \times 10^6 \) m.
   a. What is the orbital period of Deimos?
   b. At what height above the surface of Mars would a satellite have to be placed so that it remains above the same location on the surface of Mars as the planet rotates below it. A Martian day is equal to 1.02 Earth days.

Homework

35. Compute:
   a. The velocity of an object orbiting at a distance of \( 8.5 \times 10^9 \) m from the center of a spherical object whose mass is \( 5.0 \times 10^{28} \) kg.
   b. Compute the orbital period of that object.

36. Compute:
   a. The velocity of an object orbiting at height of \( 2 R_E \) above the surface of Earth.
   b. Compute the orbital period of that object.

37. Earth orbits the sun in 365.25 days and has an orbital radius of \( 1.5 \times 10^{11} \) m.
   a. How many days will it take Mercury to orbit the sun given that its orbital radius is \( 5.8 \times 10^10 \) m.
   b. How many days will it take Mars to orbit the sun given that its orbital radius is \( 2.3 \times 10^{11} \) m.
   c. It takes Jupiter 4333 days to orbit the sun. What is its average distance from the sun?

38. Compute:
   a. The velocity of an object orbiting at a distance of \( 7.3 \times 10^8 \) m from the center of a spherical object whose mass is \( 3.0 \times 10^{27} \) kg.
   b. Compute the orbital period of that object.

39. Compute:
   a. The velocity, both magnitude and direction, of an object orbiting at a height of \( 5R_E \) above the surface of Earth
   b. Compute the orbital period of that object.

40. Calculate the orbital velocity and the period, in days, for an object orbiting the sun at distance of \( 1.5 \times 10^{11} \) m. Give the period in days (The mass of the Sun is \( 1.989 \times 10^{30} \) kg).
41. Jupiter has 16 moons. One of them, Io, has an orbital radius of \( 4.2 \times 10^8 \) m and an orbital period of 1.77 days.
   a. What is the mass of Jupiter?
b. Another moon of Jupiter, Europa, has an orbital radius of $6.7 \times 10^8$ m. What is its orbital period?

c. Another moon of Jupiter, Ganymede, has an orbital period 7.2 days. What is the radius of its orbit?

d. Jupiter rotates once every 0.41 days. At what orbital radius will a satellite maintain a constant position?

**General Problems**

42. As shown in the diagram below, a 5.0 kg space rock is located $2.5 \times 10^7$ m from the center of the earth. The mass of the earth is $6.0 \times 10^{24}$ kg.

![Diagram of Earth and Space Rock](image)

a. Determine the force of gravity acting on the space rock, due to the earth. Calculate the magnitude and state the direction.

b. Compare your answer in a) to the force of gravity acting on the earth, due to the space rock. Indicate that force on the diagram above.

c. On the diagram above, indicate the direction the space rock would accelerate if released. Label that vector “a”.

d. Calculate the acceleration the rock would experience.

e. **If instead of falling, the object were in a stable orbit, indicate on the diagram above a possible direction of its velocity. Label that vector “v”.

f. **Calculate the velocity the rock needs to be in a stable orbit.

g. **Calculate the period of the rock orbiting the earth.
43. As shown in the diagram below, a 2000 kg spacecraft is located $9.2 \times 10^6$ m from the center of the earth. The mass of the earth is $6.0 \times 10^{24}$ kg.

a. Determine the force of gravity acting on the spacecraft, due to the earth. Calculate the magnitude and state the direction.

b. Compare your answer in a) to the force of gravity acting on the earth, due to the spacecraft. Indicate that force on the diagram above.

c. On the diagram above, indicate the direction the spacecraft would accelerate if released. Label that vector "a".

d. Calculate the acceleration the spacecraft would experience.

e. **If instead of falling, the spacecraft were in a stable orbit, indicate on the diagram above a possible direction of its velocity. Label that vector “v”.

f. **Calculate the velocity the spacecraft needs to be in a stable orbit.

g. **Calculate the period of the spacecraft orbiting the earth.
44. As shown in the diagram below, a 1000 kg asteroid is located 6.8x10^6 m from the center of the Mars. The mass of the Mars is 6.4x10^{23} kg.

![Diagram of Mars and Asteroid](image)

Mars

Asteroid

a. Determine the force of gravity acting on the asteroid, due to the Mars. Calculate the magnitude and state the direction.

b. Compare your answer in a) to the force of gravity acting on the Mars, due to the asteroid. Indicate that force on the diagram above.

c. On the diagram above, indicate the direction the asteroid would accelerate if released. Label that vector "a".

d. Calculate the acceleration the asteroid would experience.

e. **If instead of falling, the asteroid were in a stable orbit, indicate on the diagram above a possible direction of its velocity. Label that vector “v”.

f. **Calculate the velocity the asteroid needs to be in a stable orbit.

g. **Calculate the period of the asteroid orbiting the earth.
Answers

1. \(1.067 \times 10^{-8} \text{ N}\)
2. \(1.361 \times 10^{-9} \text{ N}\)
3. 0.045 m
4. 220400 kg
5. a) 9.77 N
   b) 9.77 N
   c) 9.77 m/s
   d) 1.63 \times 10^{-24} \text{ m/s}^2
6. 0.000356 N or 3.56 \times 10^{-4} \text{ N}
7. 0.000736 N or 7.36 \times 10^{-4} \text{ N}
8. 113.229 m
9. 40640 kg
10. a) 272 N
    b) 272 N
    c) 272 m/s
    d) 1.36 \times 10^{-28} \text{ m/s}^2
11. 1.19 \times 10^{-6} \text{ N}
12. 2.53 \times 10^{-18} \text{ N}
13. 1.50 m
14. 220400 kg
15. a) 1.71 N
    b) 1.71 N
    c) 1.71 m/s
    d) 2.31 \times 10^{-23} \text{ m/s}^2
16. 0.0099 m/s
17. 1.71 m/s
18. 2.44 m/s
19. 272 m/s
20. 3.69 m/s
21. 2.44 m/s
22. 1.09 m/s
23. 78.2 m/s
24. 0.0462 m/s
25. 0.375 m/s
26. 3.82 m/s
27. 9.08 m/s
28. 25.13 m/s
29. 0.392 m/s
30. 0.27 m/s
31. 4.89 m/s
32. a) 670 m/s
    b) \(4.2 \times 10^5 \text{ s}\)
33. 5591.57 m/s
    b) \(1.44 \times 10^4 \text{ s}\)
34. a) 1.6 days
    b) 2.04 \times 10^7 \text{ m}
35. a) \(2.0 \times 10^4 \text{ m/s}\)
    b) \(2.7 \times 10^6 \text{ s}\)
36. a) 4560 m/s
    b) \(5.09 \times 10^3 \text{ s}\)
37. a) 88 days
    b) 693.5 days
    c) \(7.8 \times 10^{11} \text{ m}\)
38. a) \(1.66 \times 10^4 \text{ m/s tangential to orbit}\)
    b) \(2.79 \times 10^5 \text{ s}\)
39. a) \(3230 \text{ m/s tangential to orbit}\)
    b) \(7.4 \times 10^4 \text{ s}\)
40. \(3.0 \times 10^4 \text{ m/s; 365 days}\)
41. a) \(1.90 \times 10^{27} \text{ kg}\)
    b) \(3.57 \text{ days}\)
    c) \(1.07 \times 10^3 \text{ m}\)
    d) \(2.58 \times 10^7 \text{ m}\)
42. a) \(3.2 \text{ N left}\)
    b) same force to right
    c) \((\rightarrow)\text{from rock towards earth}\)
    d) \(0.64 \text{ m/s}^2\)
    e) \((\uparrow\text{ or }\downarrow)\) up or down from rock
    f) \(4000 \text{ m/s}\)
    g) \(39260 \text{ s}\)
43. a) \(9457 \text{ N left}\)
    b) same force to right
    c) \((\rightarrow)\text{from spacecraft towards earth}\)
    d) \(4.73 \text{ m/s}^2\)
    e) \((\uparrow\text{ or }\downarrow)\) up or down from spacecraft
    f) \(6595 \text{ m/s}\)
    g) \(8764 \text{ s}\)
44. a) \(923 \text{ N left}\)
    b) same force to right
    c) \((\rightarrow)\text{from asteroid towards mars}\)
    d) \(0.92 \text{ m/s}^2\)
    e) \((\uparrow\text{ or }\downarrow)\) up or down from asteroid
    f) \(2505 \text{ m/s}\)
    g) \(17052 \text{ s}\)